



HELSINGIN YLIOPISTO
HELSINGFORS UNIVERSITET
UNIVERSITY OF HELSINKI

Estimating biomass and litter production: a functional-structural perspective

Annikki Mäkelä and Harry T. Valentine^{*)}

23.3.2004

^{*)} USDA Forest Service

Faculty of Agriculture and Forestry



Background

- Regional estimates of standing biomass and carbon flows require inventory data
- Inventories were designed for efficient estimates of stemwood volume and growth
- How should the inventories be developed to provide more efficient estimation of total biomass / carbon?



Outline

- Consistencies in tree structure
 - pipe model
 - scaling of crown structure

- Applicability to biomass estimates

- BEF

- Increment and turnover

- Summary



Consistencies in tree structure

- Trees show regularities in structure
- Basis: efficient use of resources under mutual competition (evolution)

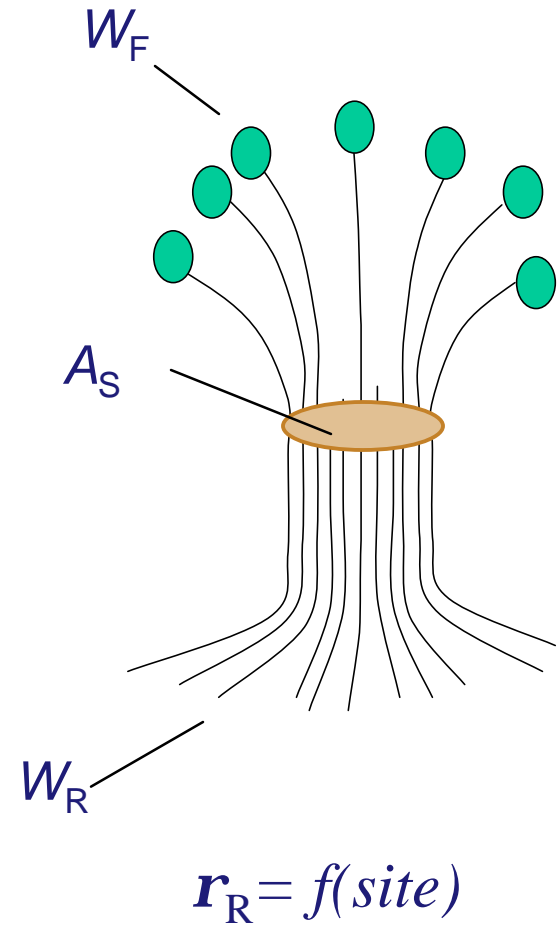


Pipe model: principle

- Shinozaki et al. 1964
- Relates foliage biomass to fine root biomass and sapwood area of stem, branches and coarse roots

$$W_F = r_S A_S$$

$$W_R = r_R A_S$$



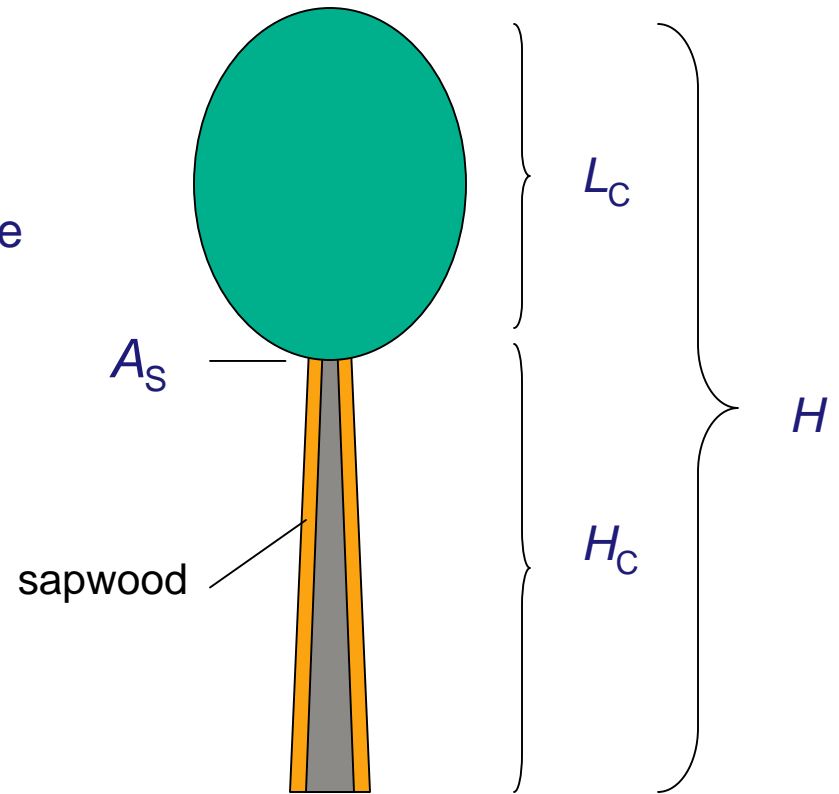


Pipe model: sapwood mass

- Mass of **live woody parts** (stem, coarse roots, branches) depends on pipe length and sapwood area:

$$W_i = r_i j_i A_S L_i$$

- Parameters:
 - r_i wood density
 - j_i form coefficient





Pipe model: average pipe length

- Stem within crown : $\varphi_C L_C$
- Stem below crown: $\varphi_S H_C = H_C$
- Branches: $\varphi_{B1} H_B = \varphi_{B2} \gamma_B L_C = \varphi_B L_C$
- Coarse roots : $\alpha_T L_{\text{stem}}$



Pipe model: bole mass

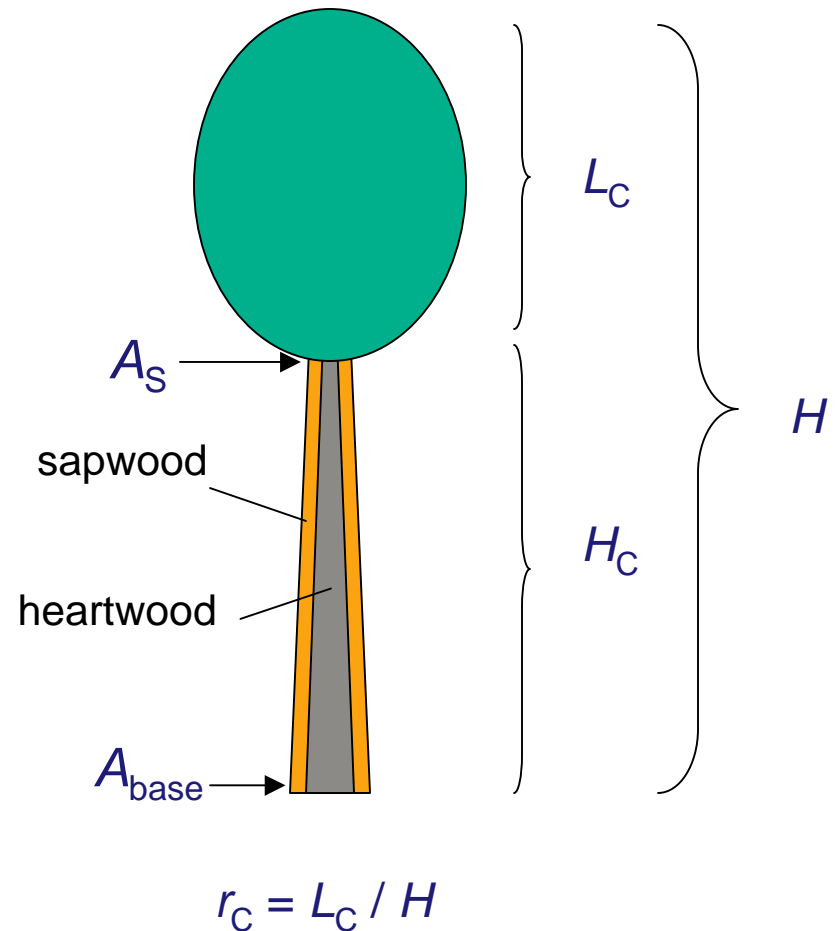
■ $W_{\text{bole}} = \text{sapwood} + \text{heartwood}$

■ $W_{\text{bole}} \approx \frac{1}{2} r_s (A_S + A_{\text{base}}) H_C$

■ Stem taper related to r_C
(Valentine 1994):

$$A_S = r_C A_{\text{base}}$$

■ $W_{\text{bole}} \approx \frac{1}{2} r_s (1 + r_C^{-1}) A_S H_C$





Pipe model: Summary

- All mass components are functions of
 - basal area at crown base (or at stem base as $A_S \approx r_C A_{\text{base}}$!)
 - tree height and crown ratio
- Crucial parameters are
 - pipe ratio of foliage and roots
 - wood density
 - form coefficients
- Applies at tree and stand level:
 - Tree or stand basal area; mean height and crown base



Crown structure: allometric scaling

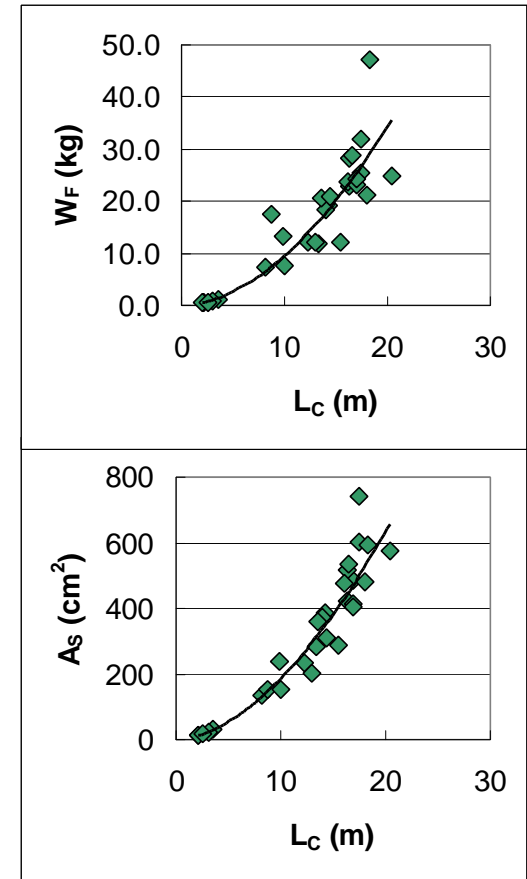
- Theoretical and empirical studies suggest an allometric scaling law between crown length and foliage mass:

$$W_F = \xi L_C^z \quad z = 3$$

Zeide and Pfeifer 1991, Mäkelä & Sievänen 1992, West et al. 1999

- Combined with pipe model:

$$A_S \propto L_C^z$$



Spruce (Kantola and Mäkelä 2003)



Crown structure: allometric scaling

- Growth rates of sapwood area and crown length scale:

$$\frac{dA_s}{dt} = z \frac{A_s}{L_c} \frac{dL_c}{dt}$$

- Also crown length is a function of sapwood area
- Additional parameter z



Applicability of structural consistencies to biomass estimates

- Parameter estimates available for several species :
 - **pine** (e.g. Berninger and Nikinmaa 1994, Vanninen 2004)
 - **birch** (Ilomäki et al. 2003)
 - **spruce** (Kantola and Mäkelä 2003)
 - **loblolly pine** (Valentine et al. 1995)

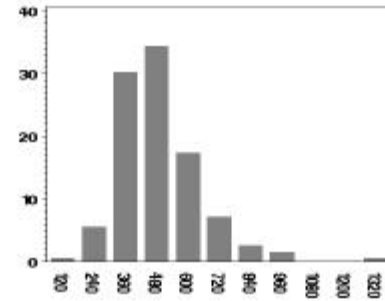
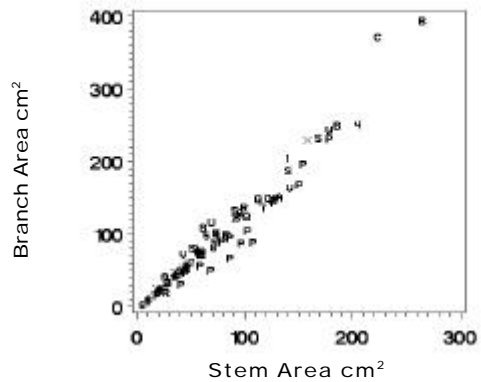
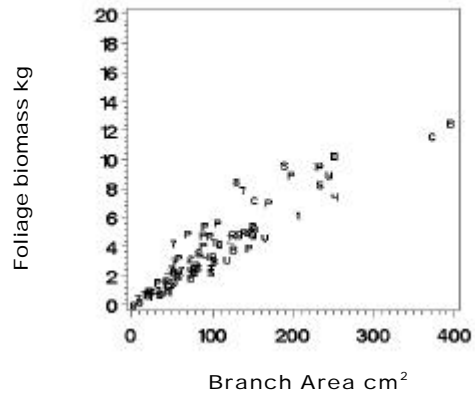
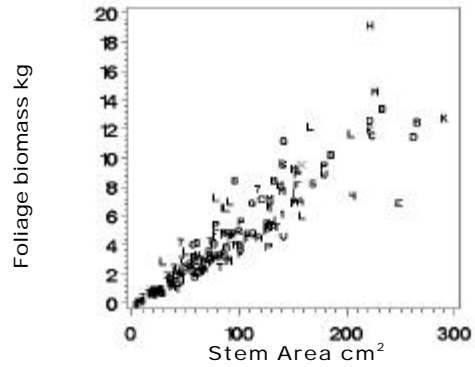
- Constant within stands

- Variation between stands:
 - small temporal trend (e.g. Mäkelä and Vanninen 1998)
 - variation between sites (Berninger et al. manus)
 - geographical trend (Berninger and Nikinmaa 1994)

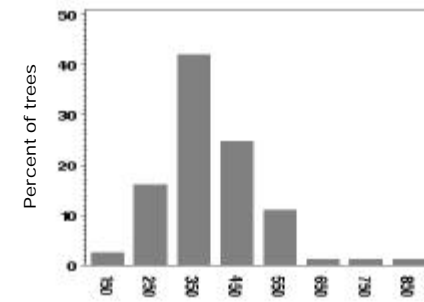


Variation in pipe ratio (pine)

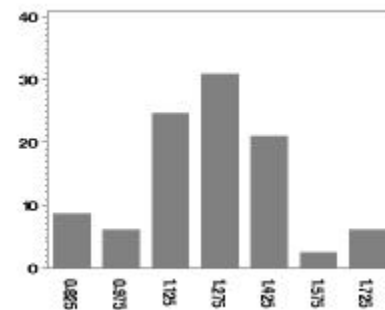
Berninger et al. manus.



Foliage to Stem area ratio kg m⁻²



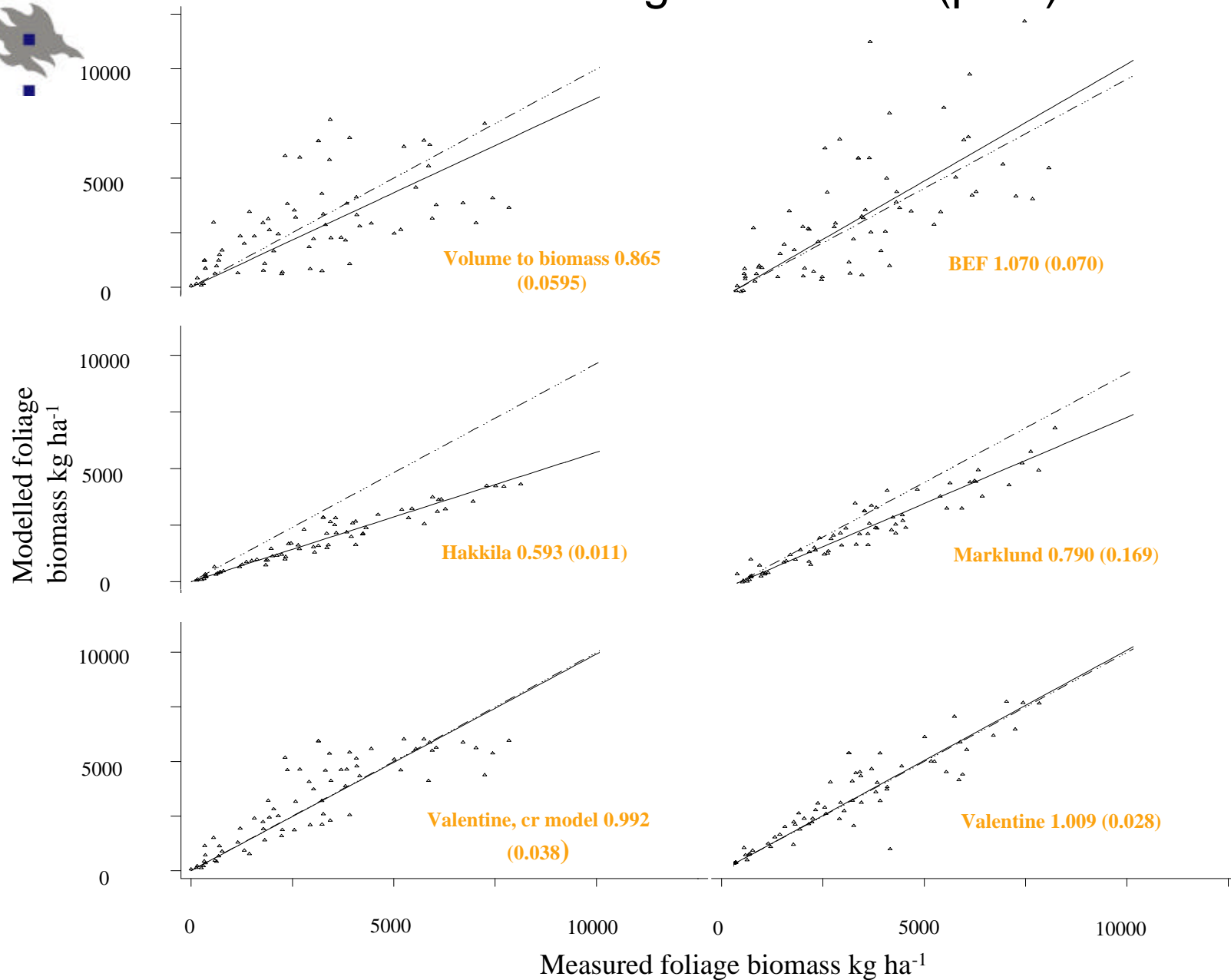
Foliage to Branch area ratio kg m⁻²



Branch area to Stem area ratio

Stand level: foliage estimates (pine)

Lehtonen 2004





BEF from the pipe model

- Pipe model assumptions lead to a formula for Biomass Expansion Factor (BEF) where A_s cancels out:

Coarse roots Stem Branches Foliage & fine roots

BEF =
$$\frac{(1 + \alpha_T) \rho_S \left[\frac{1}{2}(1 - r_C^2)/r_C + r_C \phi_C \right] + r_C \rho_B \phi_B + (\rho_F + \rho_R)/H}{\left[\frac{1}{2}(1 - r_C^2)/r_C + r_C \phi_C \right]}$$

Stem volume



BEF from the pipe model

- BEF from height, crown ratio, and parameters
- Biomass components from BEF and volume V

$$W_i = \text{BEF}_i V$$

- For trees or stands



BEF from the pipe model: parameters

Pine:
Vanninen 2003

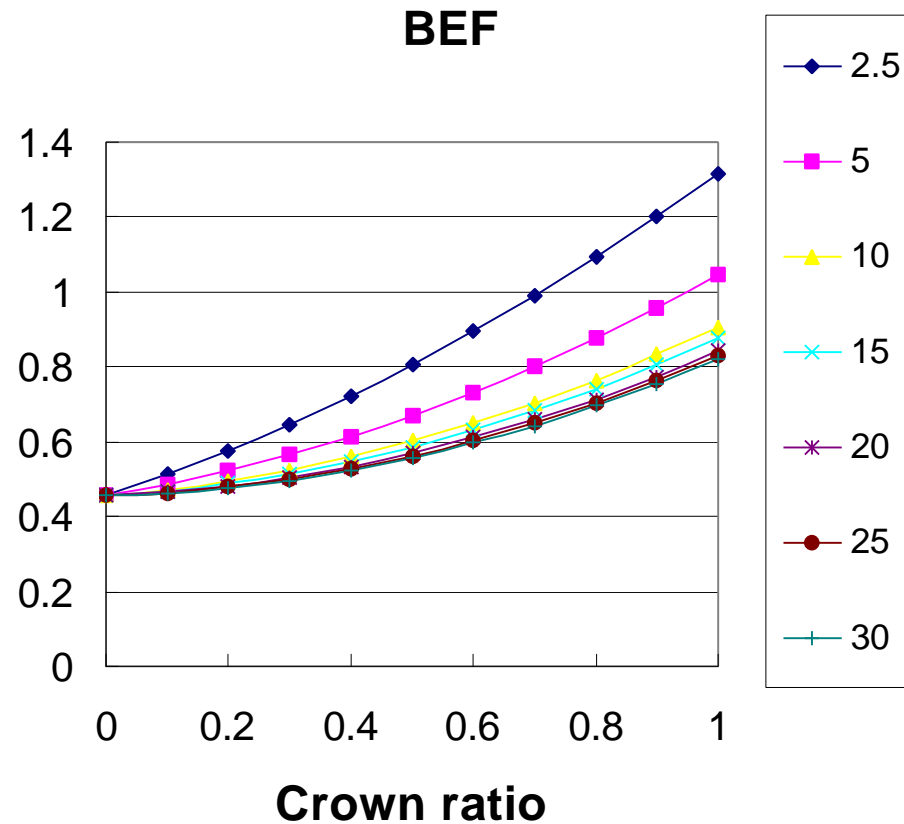
Birch:
Ilomäki et al. 2003

Parameter	Unit	Pine	Birch
pipe ratio, foliage	kg/m ²	450	255
pipe ratio, fine roots	kg/m ²	135-360	NA
wood density, stem	kg/m ³	400	480
wood density, branches	kg/m ³	400	550
stem form in crown	-	0.5	0.44
branch form	-	0.33	0.16
coarse root fraction	-	0.3	NA



BEF from the pipe model: example (pine)

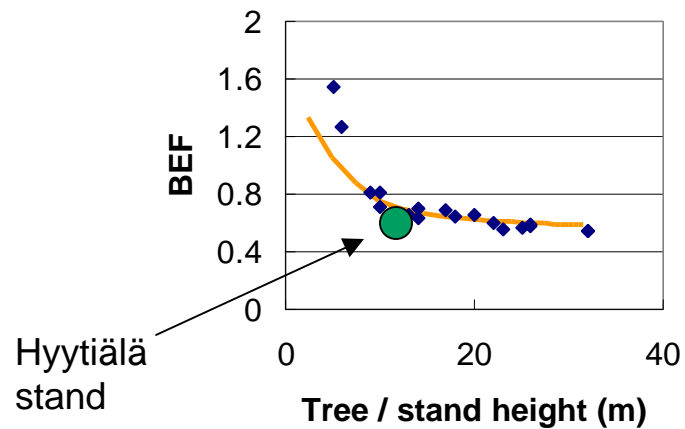
■ Parameters from Vanninen 2003



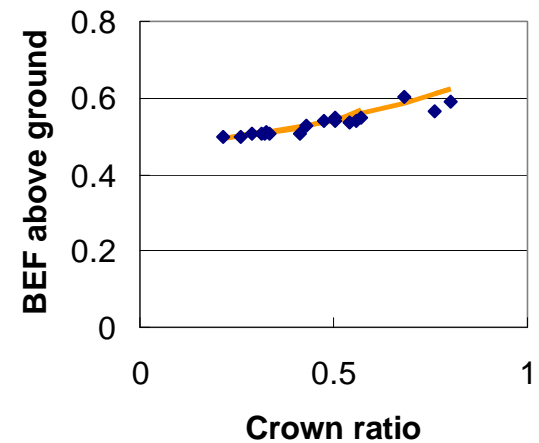


BEF from the pipe model: pine and birch

Dominant pine trees
along an age gradient,
MT & CT
Vanninen et al. 1996



Birch in varying
densities
Ilomäki et al. 2003





Increment and turnover

- NPP = Increment + Turnover

- Increment from consecutive estimates of mass:

$$\Delta W_i = \text{BEF}_{i,t+1} V_{t+1} - \text{BEF}_{i,t} V_t$$

- Component turnover from specific turnover

$$S_i = s_i \text{BEF}_i V$$

- Foliage and fine roots: mean life span is a useful concept

- Branches: not straightforward



Increment and turnover: Branch turnover

- **Pipe model** and **allometric scaling** of crown lead to an estimate of specific branch turnover rate (Valentine and Mäkelä manus):

$$s_B = \frac{(1+z)}{L_C} \frac{dH_C}{dt}$$

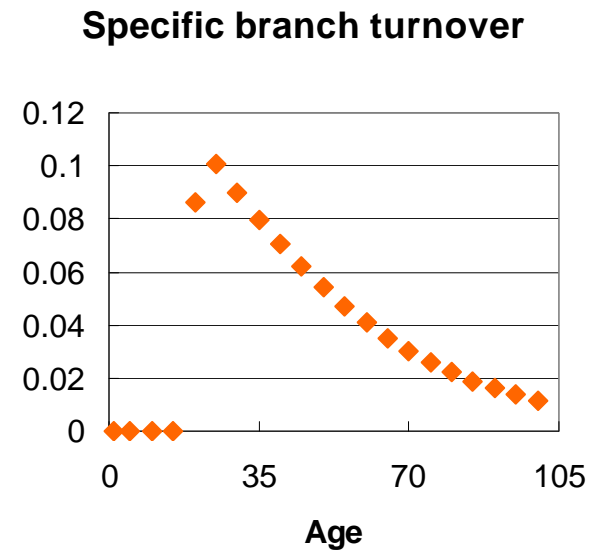
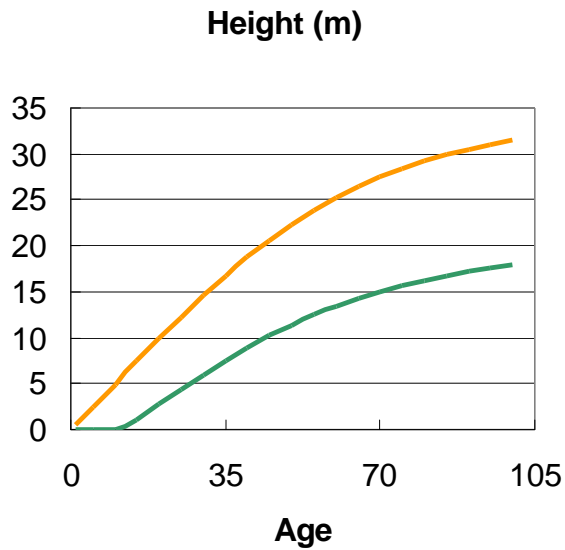
Scaling parameter

Crown length

Crown rise



Increment and turnover: Hypothetical example



Scots pine



Summary

- Structural consistencies are a powerful tool for estimating biomass, biomass increment and turnover
- Even estimates of GPP obtainable provided that live tissue specific respiration rates are available
- Requirements for wider application
 - crown ratio from inventories
 - more information on the natural variation of parameters
 - allows for focused measurements with physical meaning
- But: BEF estimates rather stable under variation of parameters and tree attributes